



22097306



MATHEMATICS
STANDARD LEVEL
PAPER 2

Friday 8 May 2009 (morning)

1 hour 30 minutes

Candidate session number

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INSTRUCTIONS TO CANDIDATES

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Section A: answer all of Section A in the spaces provided.
- Section B: answer all of Section B on the answer sheets provided. Write your session number on each answer sheet, and attach them to this examination paper and your cover sheet using the tag provided.
- At the end of the examination, indicate the number of sheets used in the appropriate box on your cover sheet.
- Unless otherwise stated in the question, all numerical answers must be given exactly or correct to three significant figures.



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13 pages

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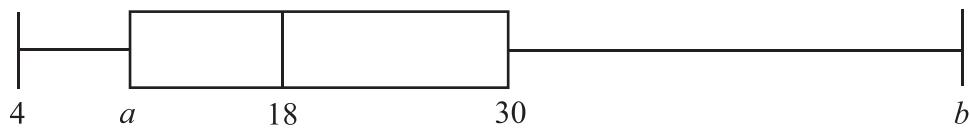
Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. In particular, solutions found from a graphic display calculator should be supported by suitable working, e.g. if graphs are used to find a solution, you should sketch these as part of your answer. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

SECTION A

Answer all the questions in the spaces provided. Working may be continued below the lines, if necessary.

1. [Maximum mark: 5]

The following diagram is a box and whisker plot for a set of data.



The interquartile range is 20 and the range is 40.

- (a) Write down the median value. [1 mark]

(b) Find the value of

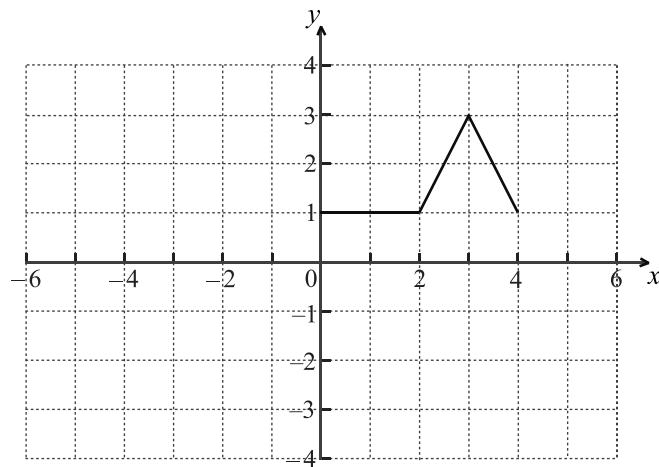
(i) a ;

(ii) b . [4 marks]



2. [Maximum mark: 6]

Consider the graph of f shown below.



- (a) On the **same** grid sketch the graph of $y = f(-x)$. [2 marks]

(This question continues on the following page)



(Question 2 continued)

The following four diagrams show **images** of f under different transformations.

Diagram A

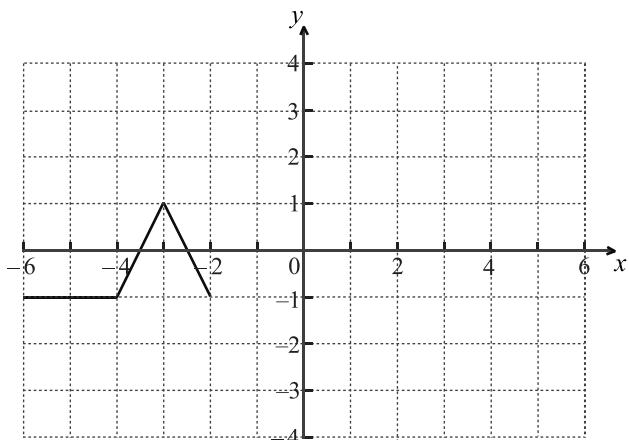


Diagram B

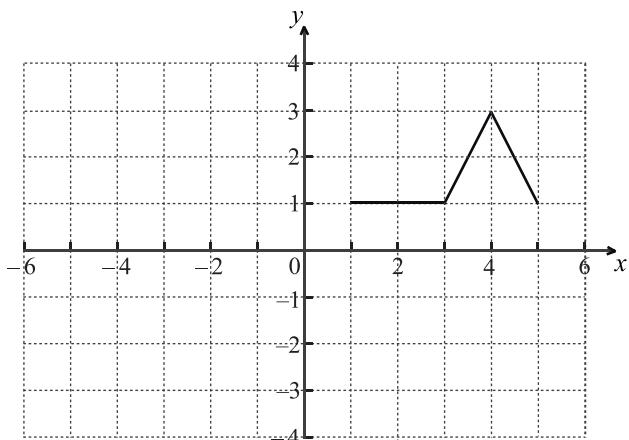


Diagram C

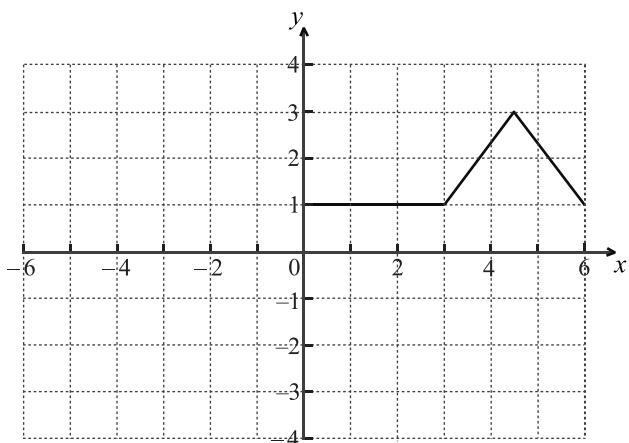
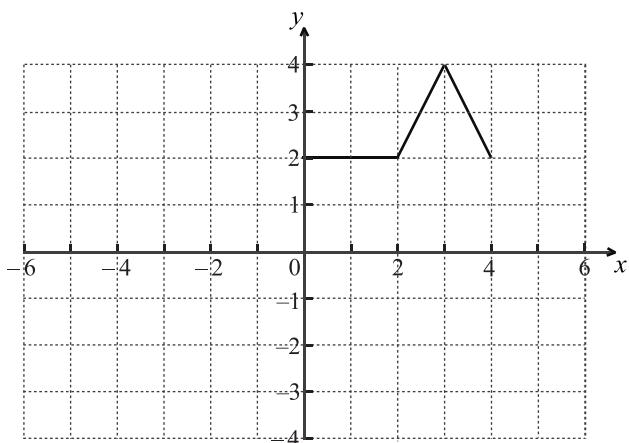


Diagram D



- (b) Complete the following table.

[2 marks]

Description of transformation	Diagram letter
Horizontal stretch with scale factor 1.5	
Maps f to $f(x)+1$	

- (c) Give a full geometric description of the transformation that gives the image in Diagram A.

[2 marks]

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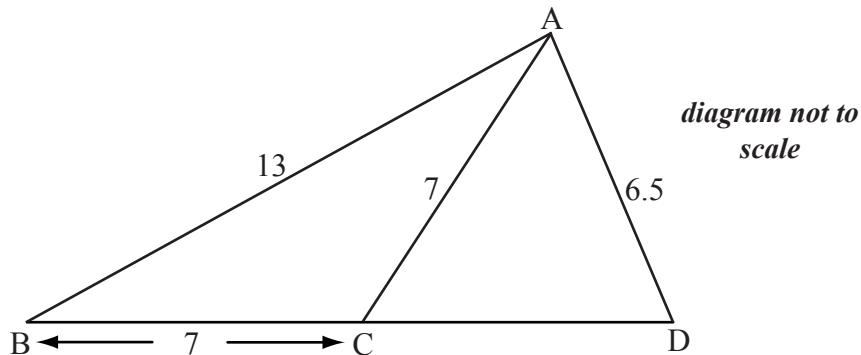
- 3.** [Maximum mark: 5]

Solve the equation $e^x = 4 \sin x$, for $0 \leq x \leq 2\pi$.



4. [Maximum mark: 8]

The diagram below shows a triangle ABD with $AB = 13 \text{ cm}$ and $AD = 6.5 \text{ cm}$. Let C be a point on the line BD such that $BC = AC = 7 \text{ cm}$.



- (a) Find the size of angle ACB. [3 marks]

(b) Find the size of angle CAD. [5 marks]



5. [Maximum mark: 7]

- (a) Expand $\sum_{r=4}^7 2^r$ as the sum of four terms. [1 mark]

(b) (i) Find the value of $\sum_{r=4}^{30} 2^r$.

(ii) Explain why $\sum_{r=4}^{\infty} 2^r$ cannot be evaluated. [6 marks]



6. [Maximum mark: 7]

Consider the curve $y = \ln(3x-1)$. Let P be the point on the curve where $x = 2$.

- (a) Write down the gradient of the curve at P. [2 marks]

(b) The normal to the curve at P cuts the x -axis at R. Find the coordinates of R. [5 marks]



7. [Maximum mark: 7]

The quadratic equation $kx^2 + (k - 3)x + 1 = 0$ has two equal real roots.

- (a) Find the possible values of k . [5 marks]

(b) Write down the values of k for which $x^2 + (k-3)x + k = 0$ has two equal real roots. [2 marks]



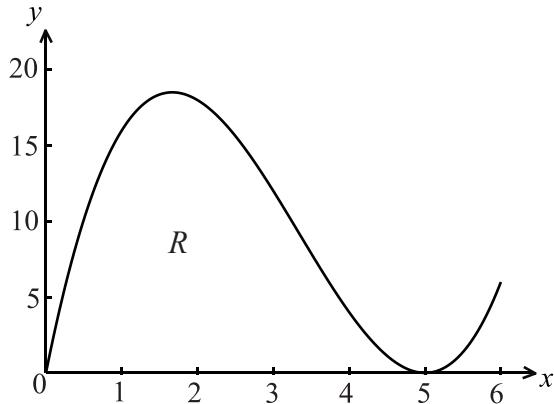
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SECTION B

Answer all the questions on the answer sheets provided. Please start each question on a new page.

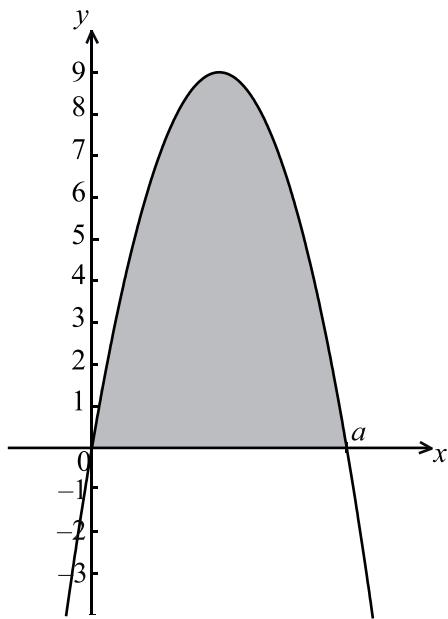
8. [Maximum mark: 14]

Let $f(x) = x(x-5)^2$, for $0 \leq x \leq 6$. The following diagram shows the graph of f .



Let R be the region enclosed by the x -axis and the curve of f .

- (a) Find the area of R . [3 marks]
- (b) Find the volume of the solid formed when R is rotated through 360° about the x -axis. [4 marks]
- (c) The diagram below shows a part of the graph of a quadratic function $g(x) = x(a-x)$. The graph of g crosses the x -axis when $x=a$.



The area of the shaded region is equal to the area of R . Find the value of a .

[7 marks]



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9. [Maximum mark: 13]

A van can take either Route A or Route B for a particular journey.

If Route A is taken, the journey time may be assumed to be normally distributed with mean 46 minutes and a standard deviation 10 minutes.

If Route B is taken, the journey time may be assumed to be normally distributed with mean μ minutes and standard deviation 12 minutes.

- (a) For Route A, find the probability that the journey takes **more** than 60 minutes. [2 marks]
- (b) For Route B, the probability that the journey takes **less** than 60 minutes is 0.85.
Find the value of μ . [3 marks]
- (c) The van sets out at 06:00 and needs to arrive before 07:00.
 - (i) Which route should it take?
 - (ii) Justify your answer. [3 marks]
- (d) On five consecutive days the van sets out at 06:00 and takes Route B. Find the probability that
 - (i) it arrives before 07:00 on all five days;
 - (ii) it arrives before 07:00 on at least three days. [5 marks]



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10. [Maximum mark: 18]

Let $f(x) = 3 \sin x + 4 \cos x$, for $-2\pi \leq x \leq 2\pi$.

- (a) Sketch the graph of f . [3 marks]
- (b) Write down
- (i) the amplitude;
 - (ii) the period;
 - (iii) the x -intercept that lies between $-\frac{\pi}{2}$ and 0. [3 marks]
- (c) Hence write $f(x)$ in the form $p \sin(qx+r)$. [3 marks]
- (d) Write down one value of x such that $f'(x) = 0$. [2 marks]
- (e) Write down the two values of k for which the equation $f(x) = k$ has exactly two solutions. [2 marks]
- (f) Let $g(x) = \ln(x+1)$, for $0 \leq x \leq \pi$. There is a value of x , between 0 and 1, for which the gradient of f is equal to the gradient of g . Find this value of x . [5 marks]
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